

# Unravelling the Pathways of Ultrafast Vibrational Energy Flow in Hydrogen Bonds

Oliver Kühn

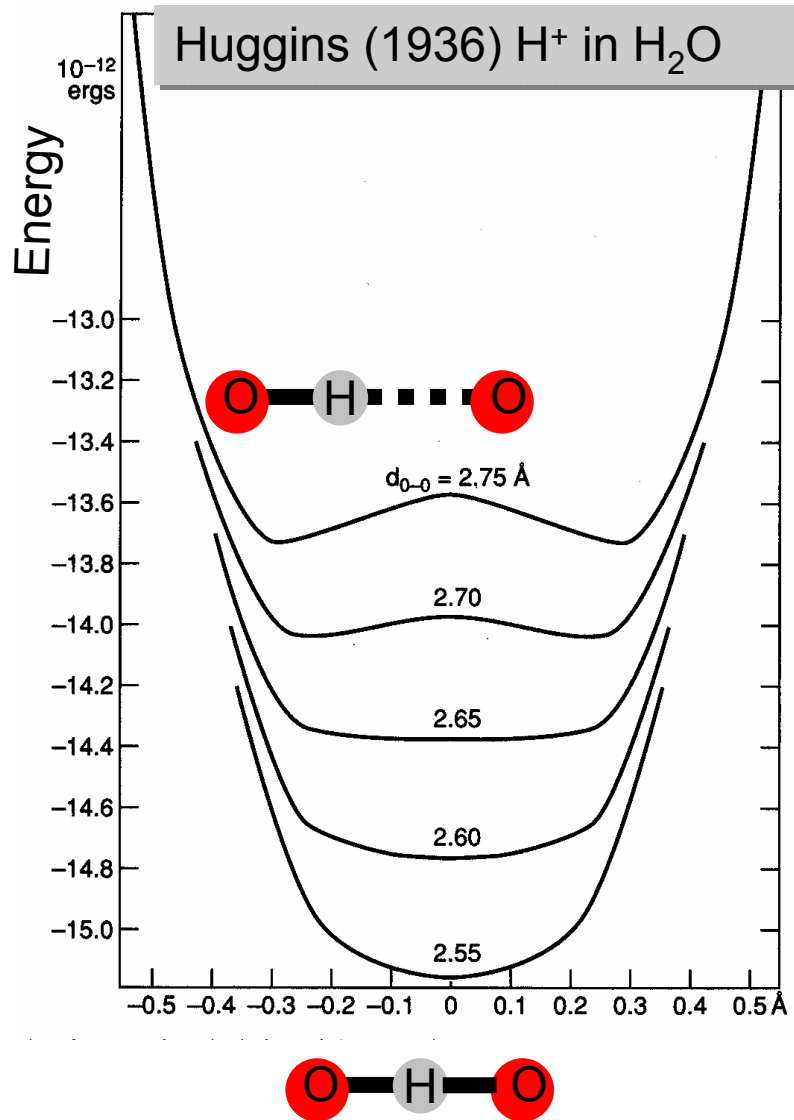
Milena Petkovic, Gireesh Krishnan

Physical and Theoretical Chemistry

Free University Berlin



# AGENDA



correlation

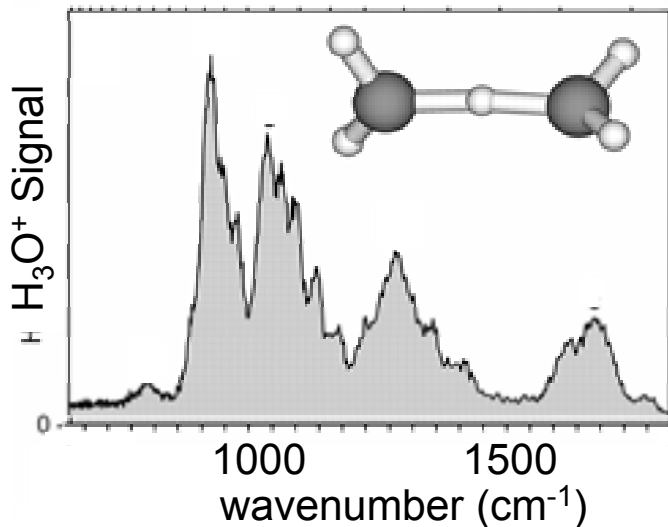
$\text{H-atom} \leftrightarrow \text{H-bond}$

multidimensional quantum  
dynamics

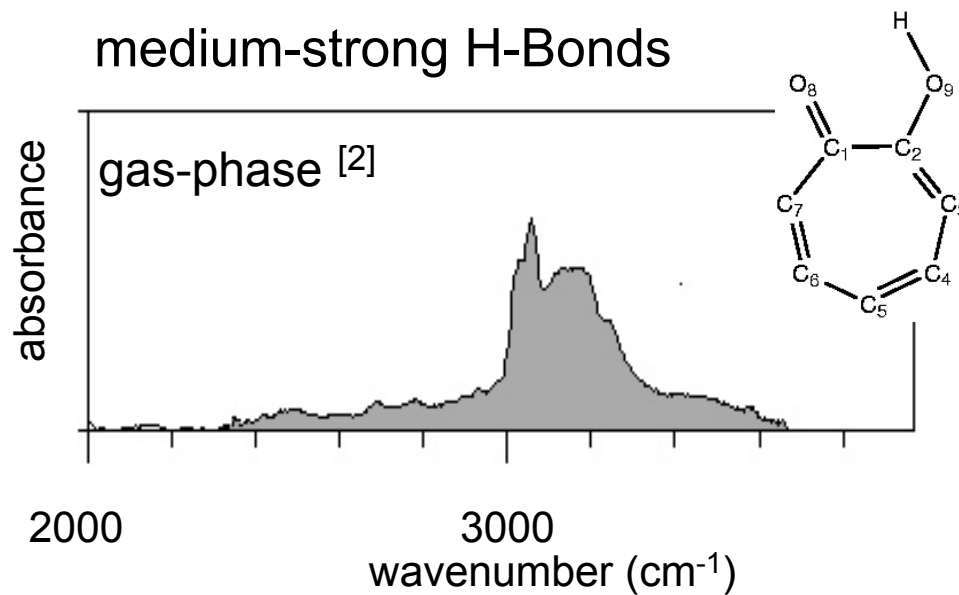
potential energy surfaces  
equations of motion

# MULTIDIMENSIONALITY & IR SPECTRUM

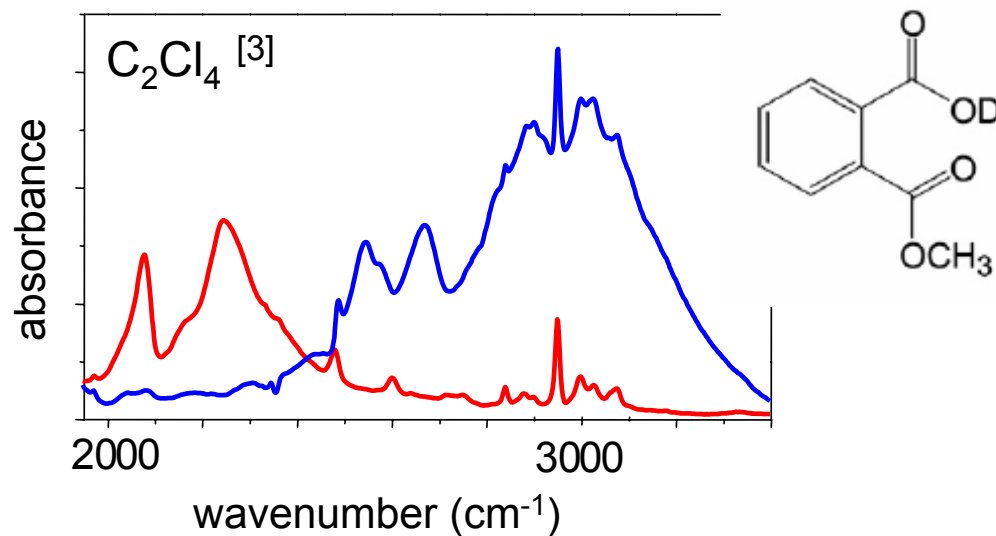
strong H-Bond [1]



medium-strong H-Bonds

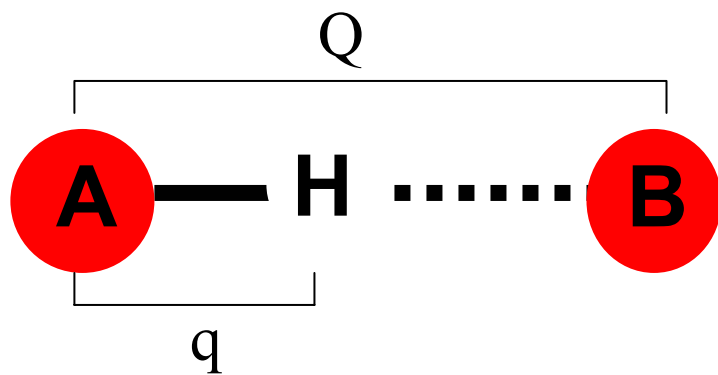


red-shift  
broadening  
substructure

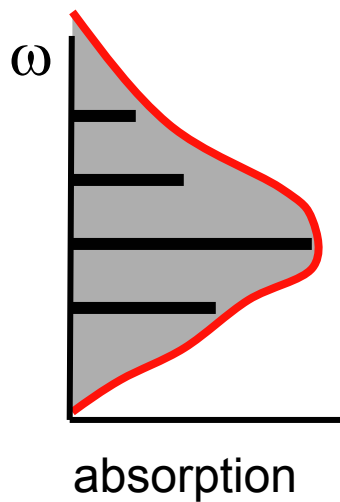


[1] K. Asmis et al., Science 299, 1375 (2003), [2] NIST, [3] J. Stenger et al. □

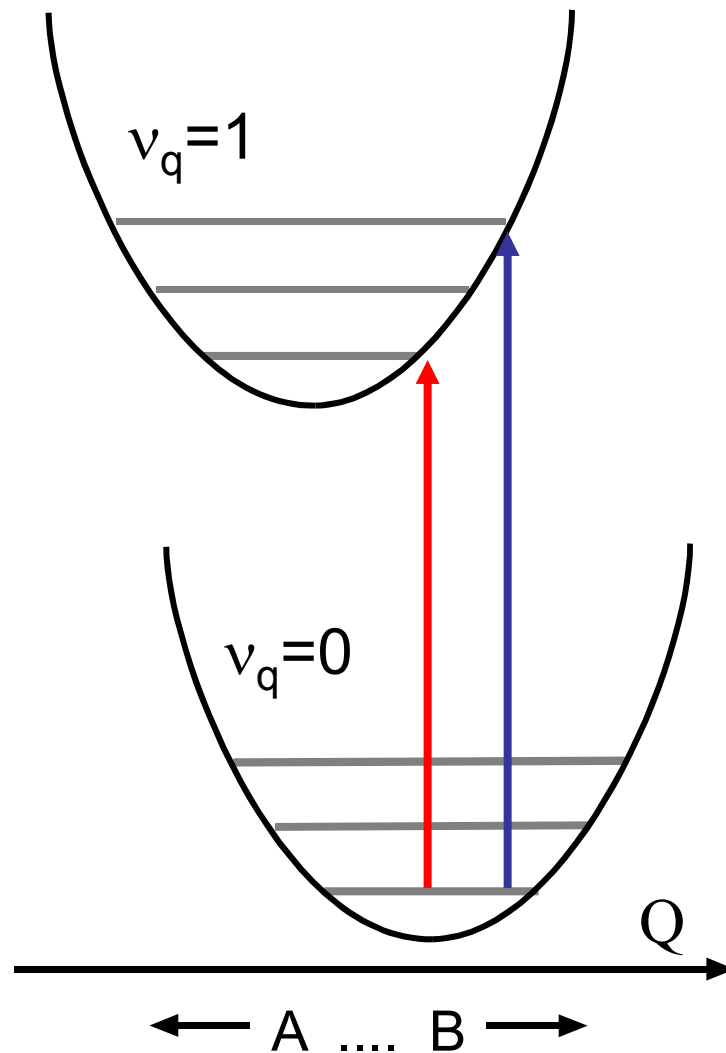
# A SIMPLE ADIABATIC MODEL



Franck-Condon-like transition

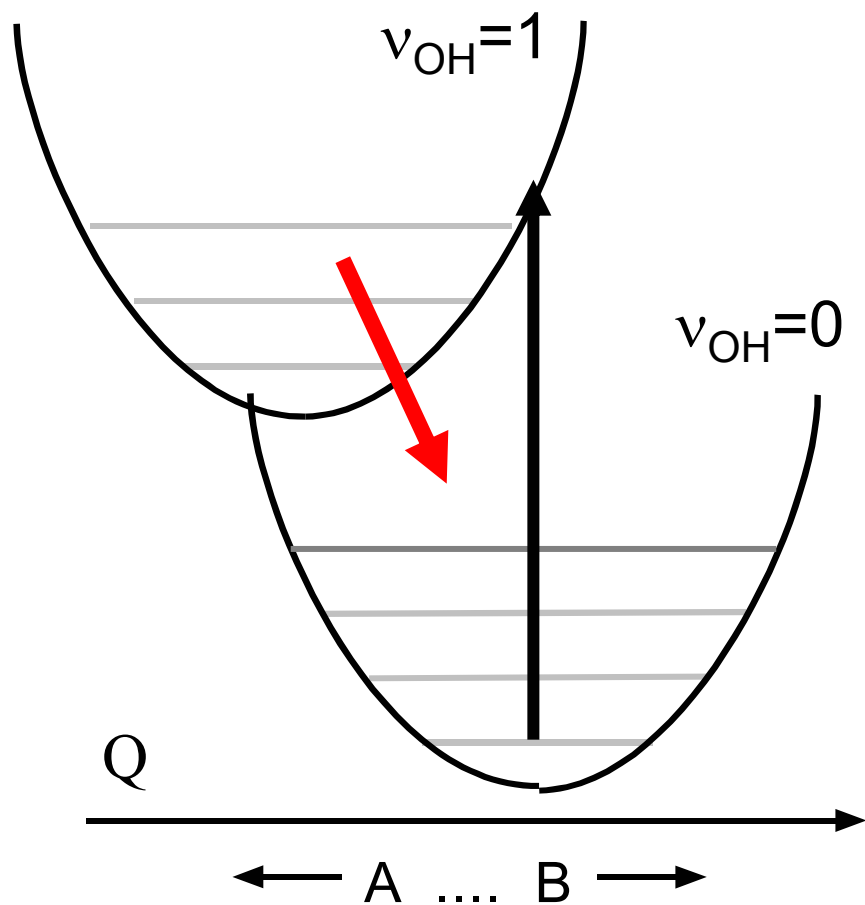


?

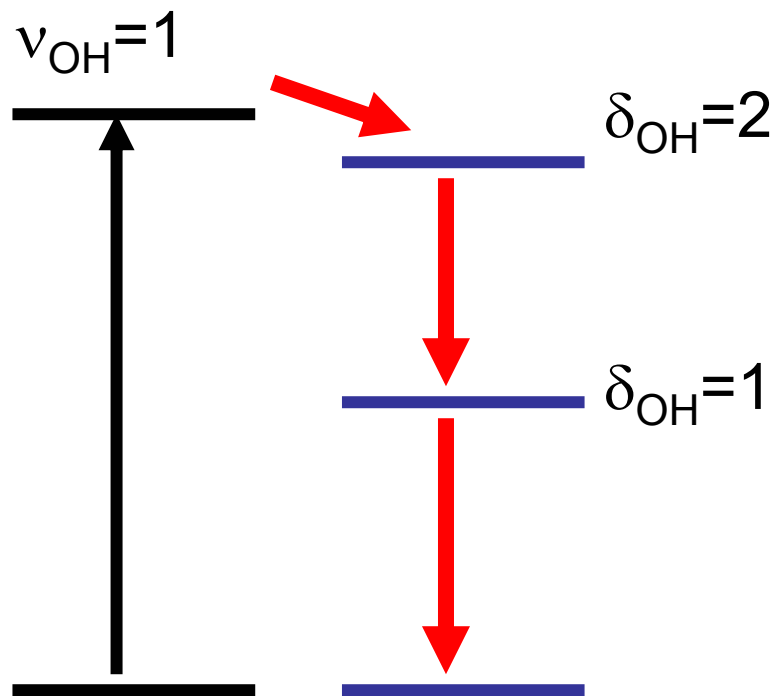


# VIBRATIONAL RELAXATION MODELS

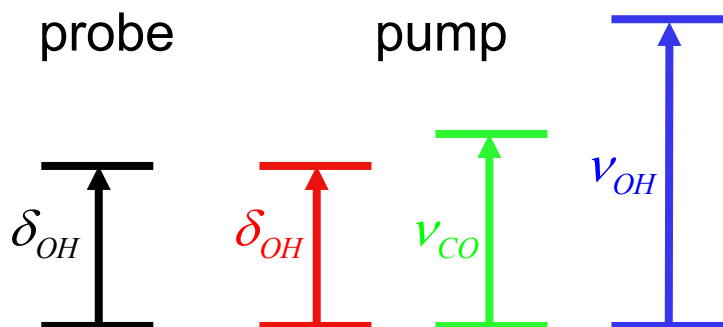
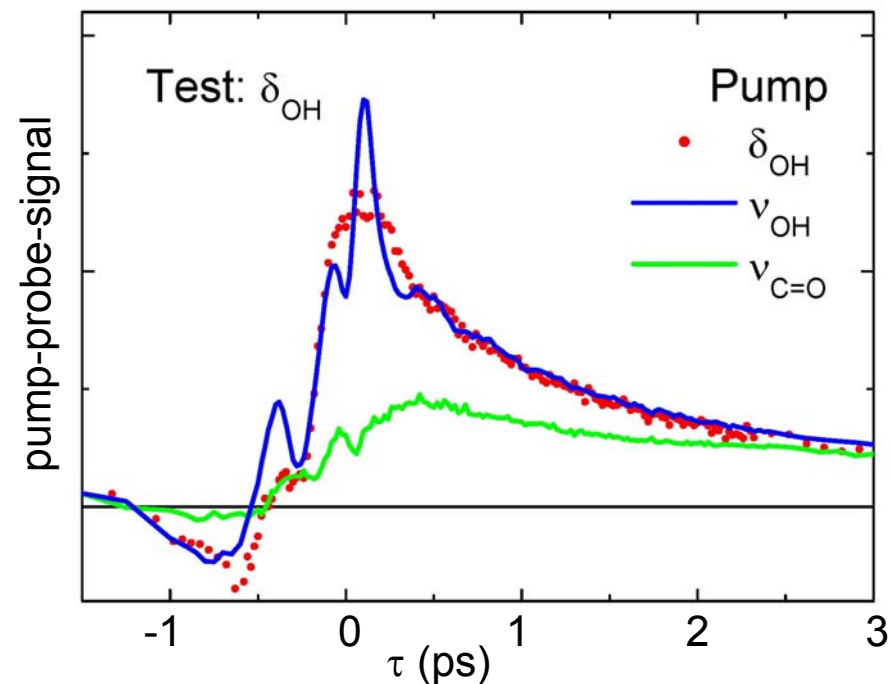
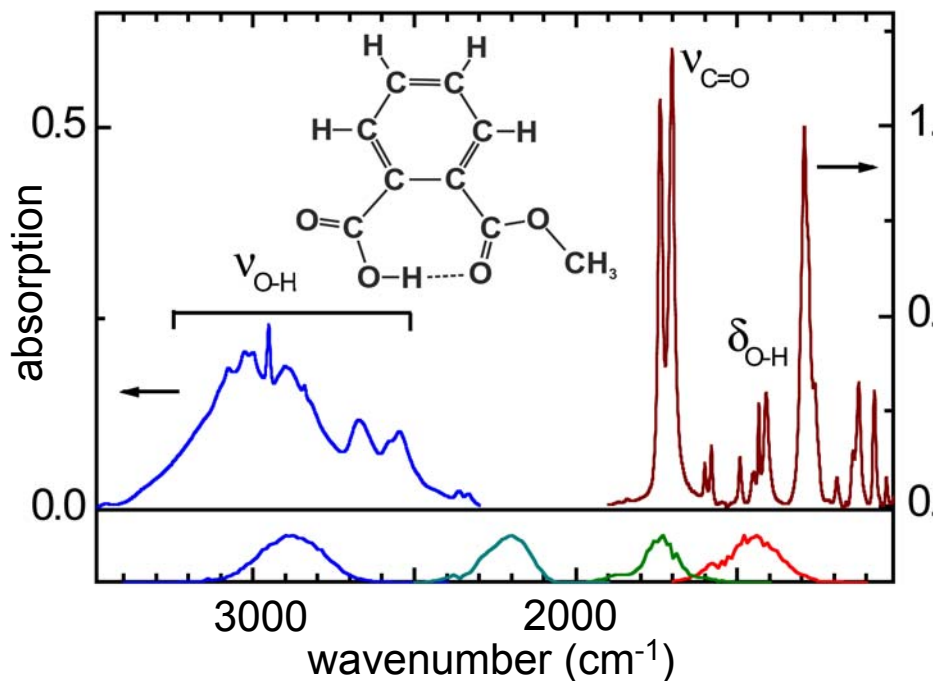
via H-bond motion



via Fermi-resonance



# PMME-H: 2-COLOR IR SPECTROSCOPY



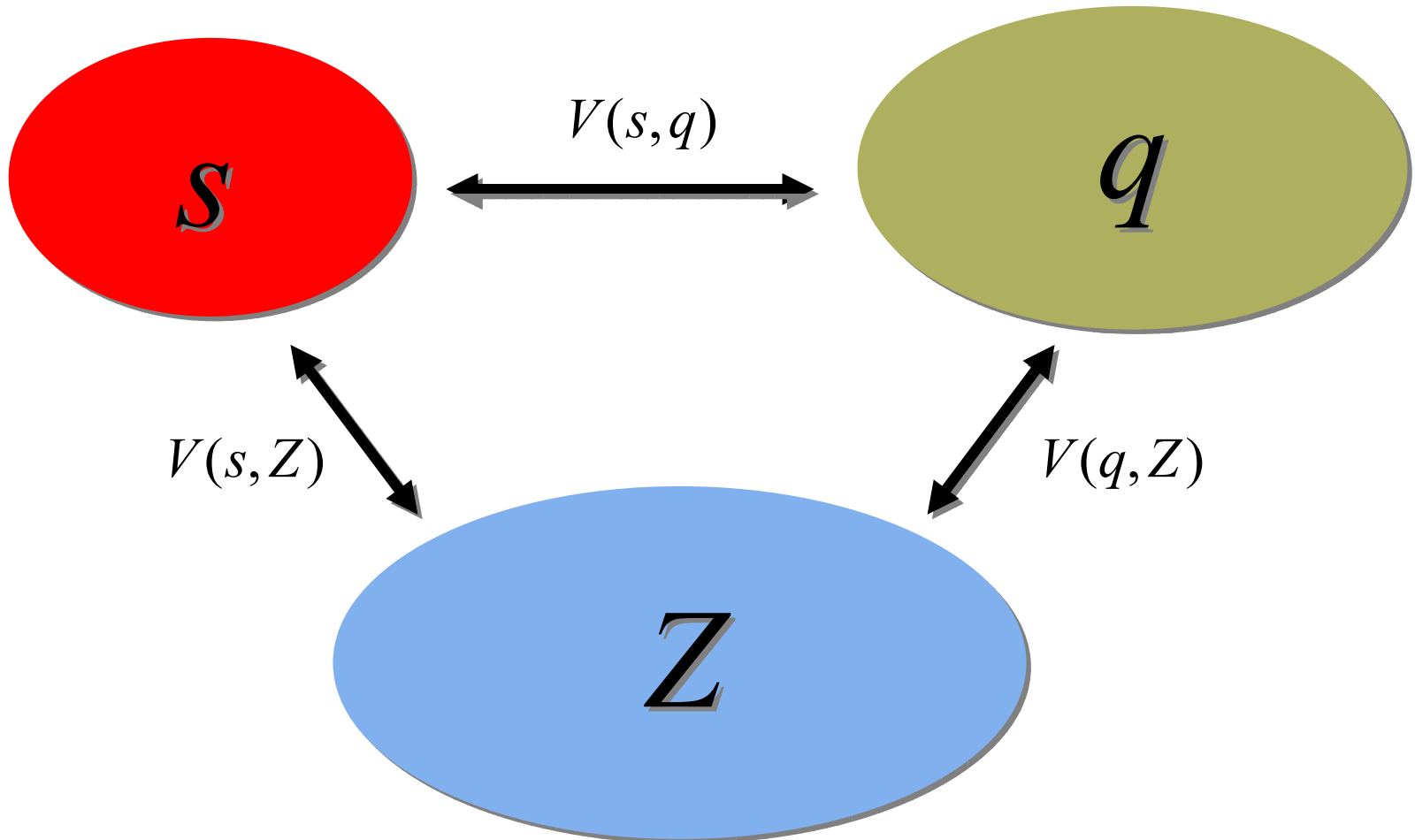
$T_1(\nu_{OH})=200\text{fs}$ ,  $T_1(\delta_{OH})=800\text{fs}$   
relaxation via  $\delta_{OH}=1$  (>30%)

$T_{\text{cool}} \sim 20 \text{ ps}$

$\nu_{\text{osc}} \sim 100 \text{ cm}^{-1}$

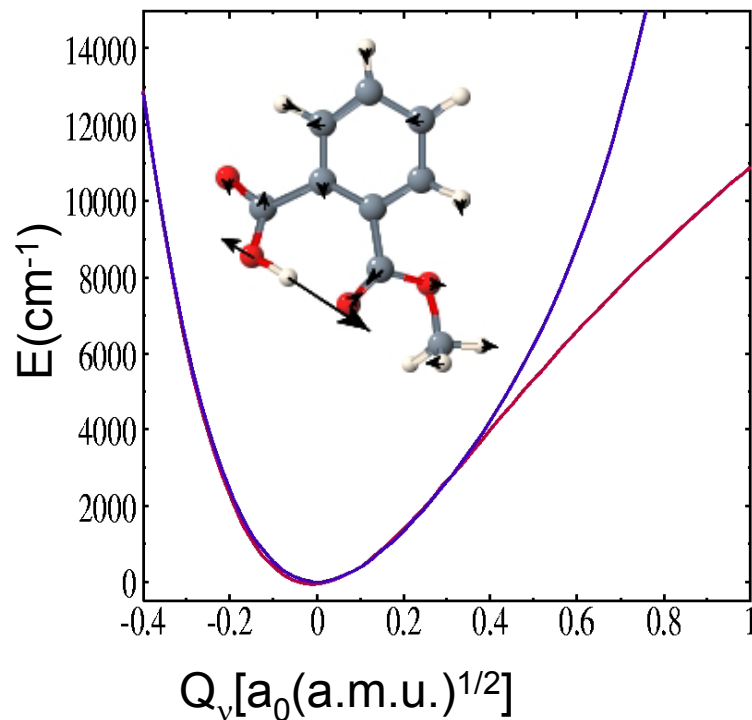
# SYSTEM-BAD APPROACH

$$H = H_{SYS}(s; t) + H_{BATH}(q, Z) + H_{SB}(s, q, Z)$$



# POTENTIAL ENERGY SURFACES

- Reaction Surface Hamiltonian
  - no proton transfer
  - no bond dissociation
- normal mode representation



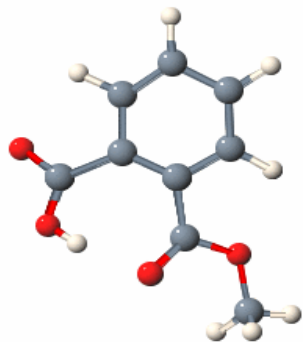
$$V(\mathbf{Q}) = \sum_i V^{(1)}(Q_i) + V_{corr}(\mathbf{Q})$$

$$V_{corr}(\mathbf{Q}) = \sum_{i \neq j} V^{(2)}(Q_i, Q_j) + \sum_{i \neq j \neq k} V^{(3)}(Q_i, Q_j, Q_k) + \sum_{i \neq j \neq k \neq l} V^{(4)}(Q_i, Q_j, Q_k, Q_l) + \dots$$

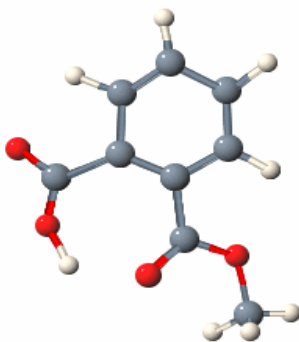
- choice of relevant coordinates
- calculation of correlation potential



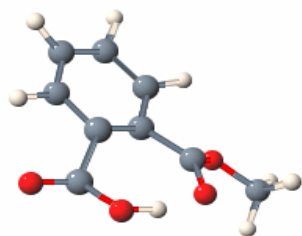
# PMME: 5D DISSIPATIVE MODEL



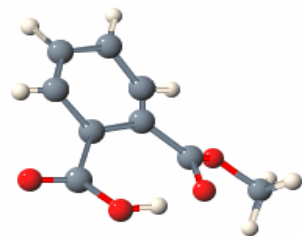
$$\nu_{\text{OH}} = 3036 \text{ cm}^{-1}$$



$$\delta_{\text{OH}} = 1455 \text{ cm}^{-1}$$



$$\gamma_1 = 792 \text{ cm}^{-1}$$



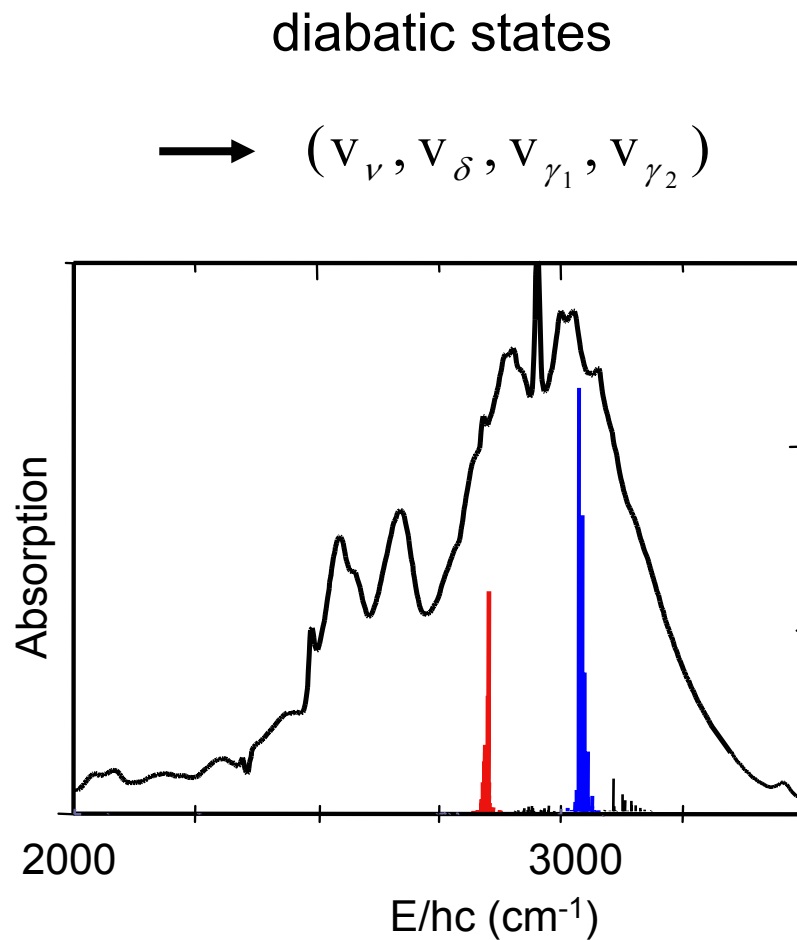
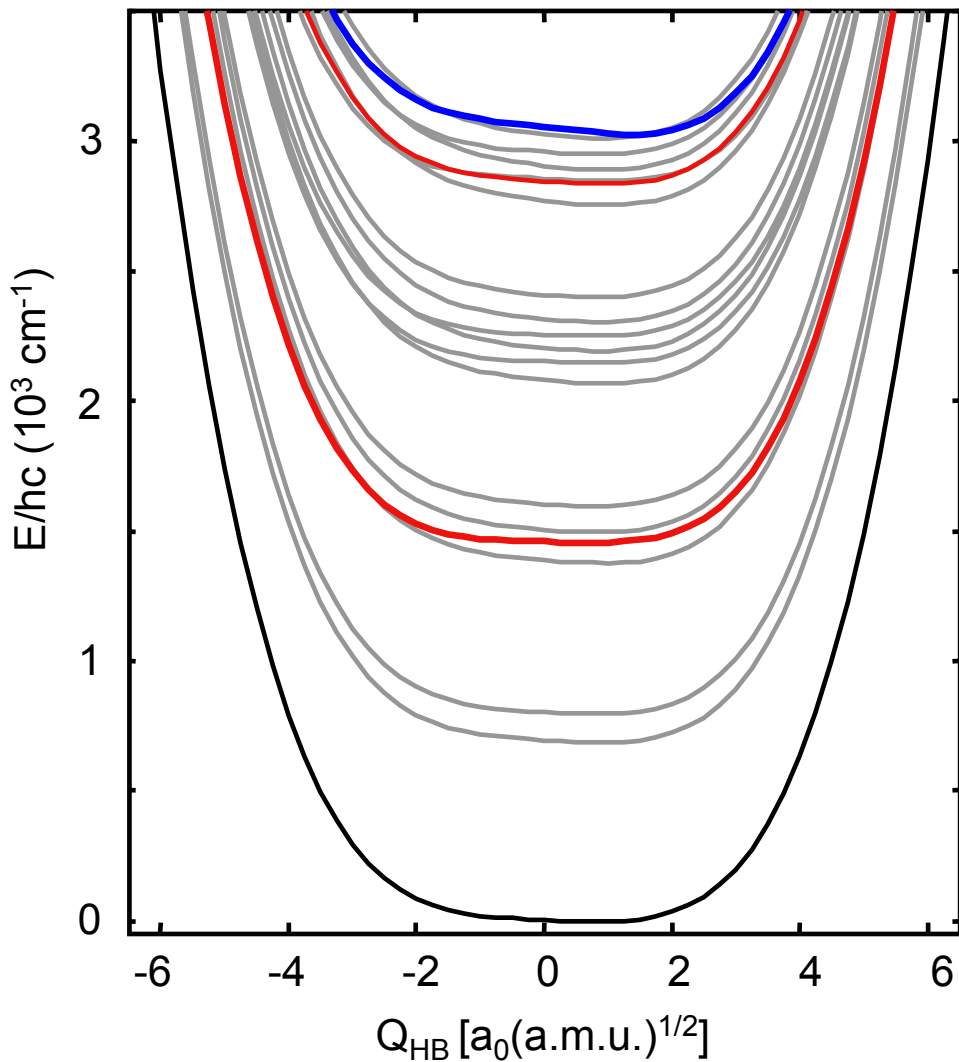
$$\gamma_2 = 690 \text{ cm}^{-1}$$



$$\nu_{\text{HB}} = 63 \text{ cm}^{-1}$$



# PMME-H: IR SPECTRUM



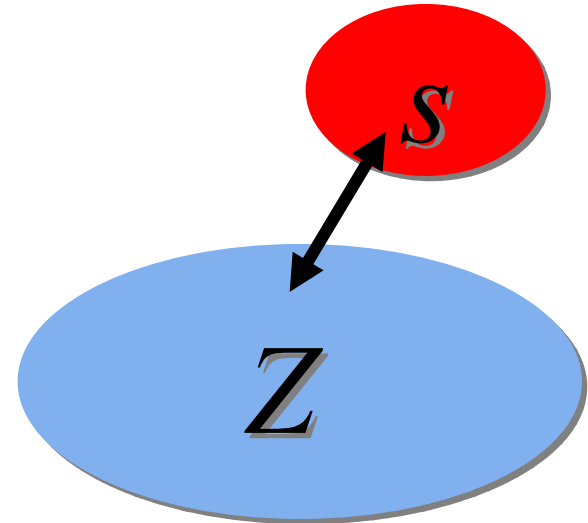
# DISSIPATIVE QUANTUM DYNAMICS

observables

$$O(s, t) = \text{tr}_{\text{SYS}} \left( \hat{O}(s) \hat{\rho}(t) \right)$$

reduced density operator

$$\hat{\rho}(t) = \text{tr}_{\text{BATH}} \left( \hat{\rho}_{\text{total}}(t) \right)$$



Quantum-Master Equation

$$\frac{\partial \rho_{ab}}{\partial t} = \underbrace{-i\omega_{ab}\rho_{ab} + iE(t) \sum_c (d_{ac}\rho_{cb} - d_{cb}\rho_{ac})}_{\text{coherent dynamics}} - \underbrace{\sum_{cd} R_{ab,cd}\rho_{cd}}_{\text{relaxation/dissipation}}$$

coherent dynamics

relaxation/dissipation

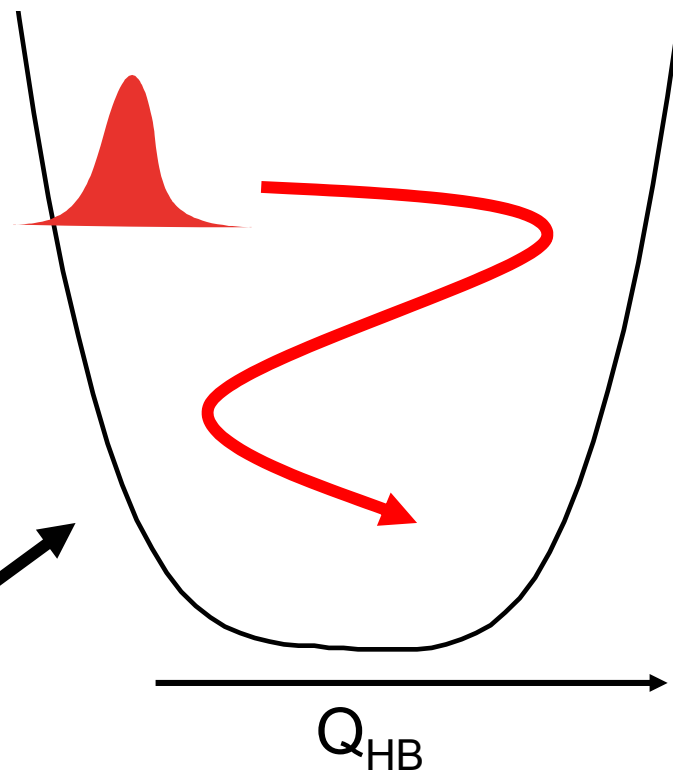
# PMME: SYSTEM-BATH MODEL

$V(s = Q, q, Z)$   relevant interactions

intramolecular  
+ solvent



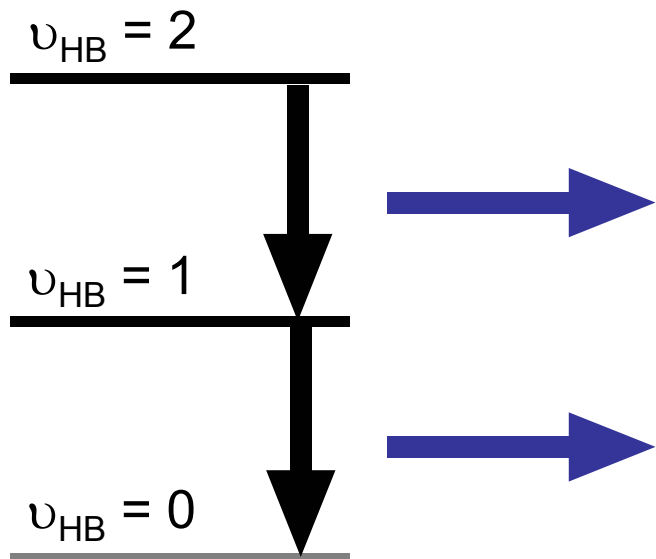
solvent



# PMME: RELAXATION OF HB-MODE

bilinear coupling

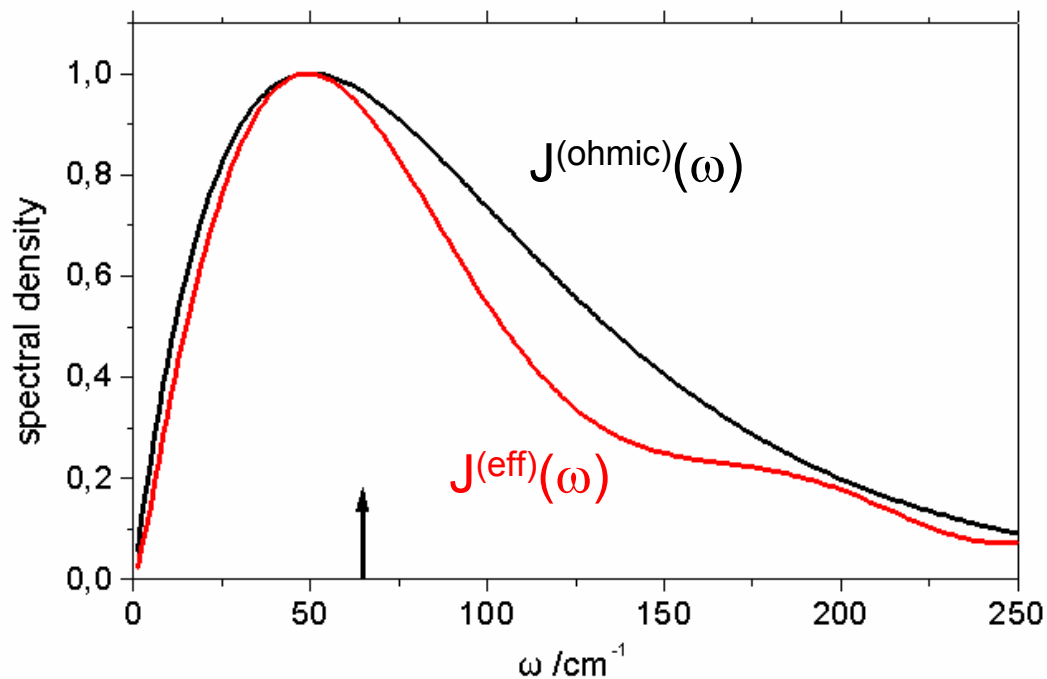
$$H_{SB}^{(I)} = Q_{HB} \sum_{\lambda} g_{HB,\lambda}^{(I)} Z_{\lambda}$$



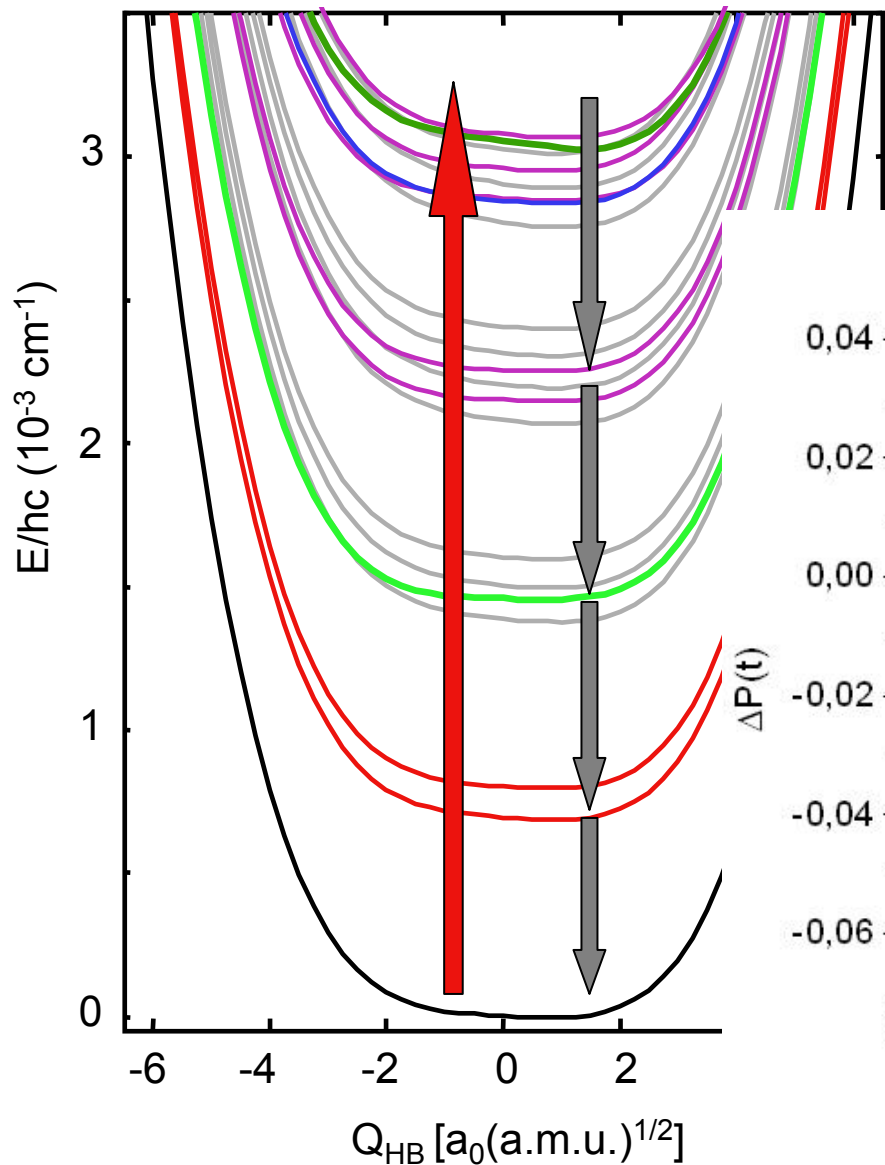
$T_1 \sim 1.6\text{ps}$

spectral density

classical MD PMME/CCl4 at  $T=300\text{K}$

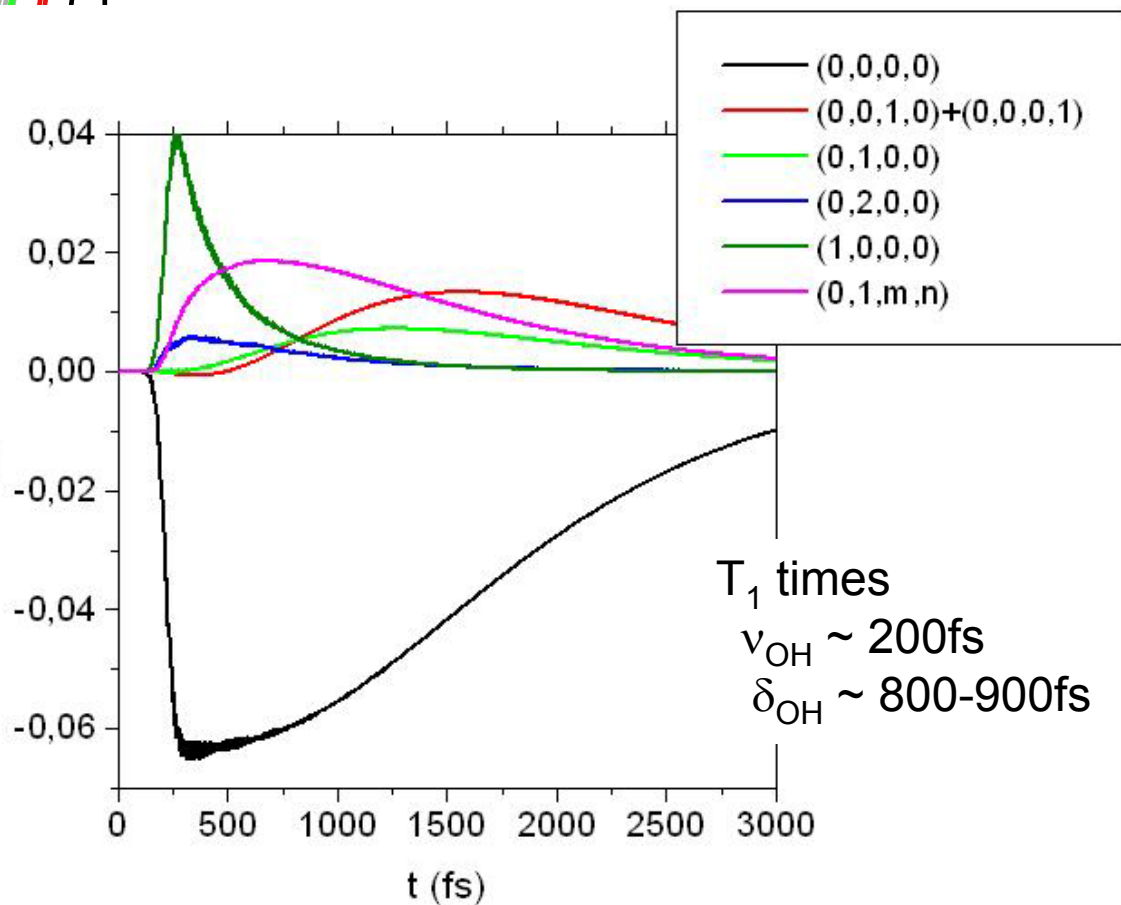


# OH-STRETCH RELAXATION

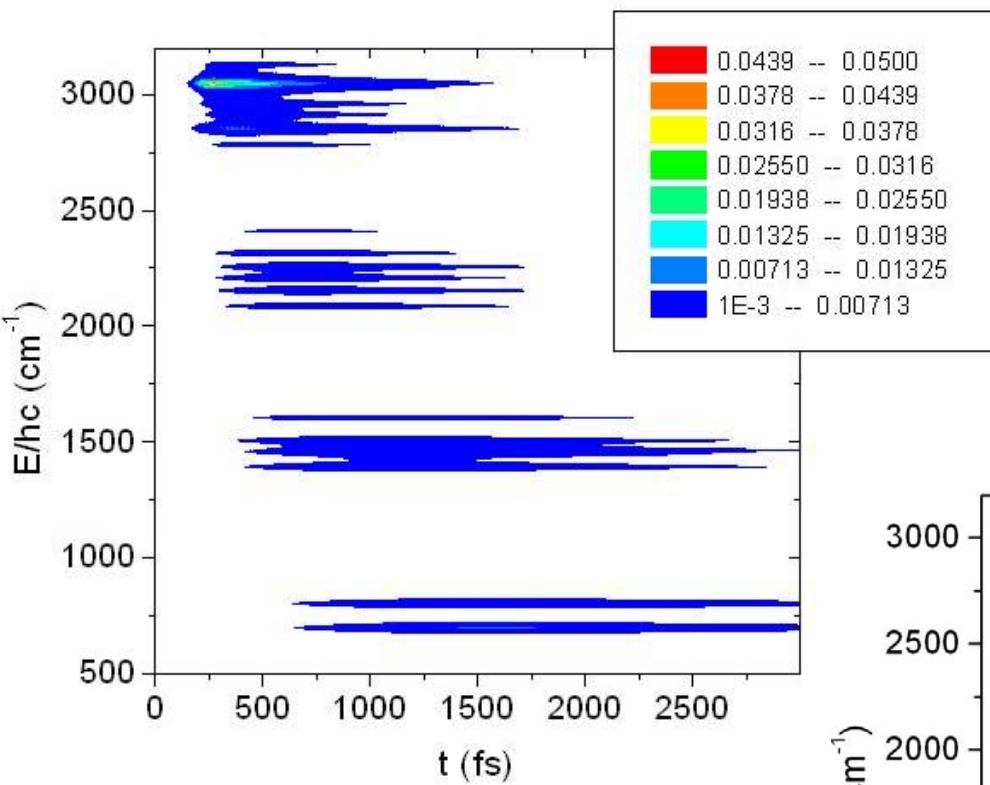


diabatic states

$$(v_\nu, v_\delta, v_{\gamma_1}, v_{\gamma_2})$$

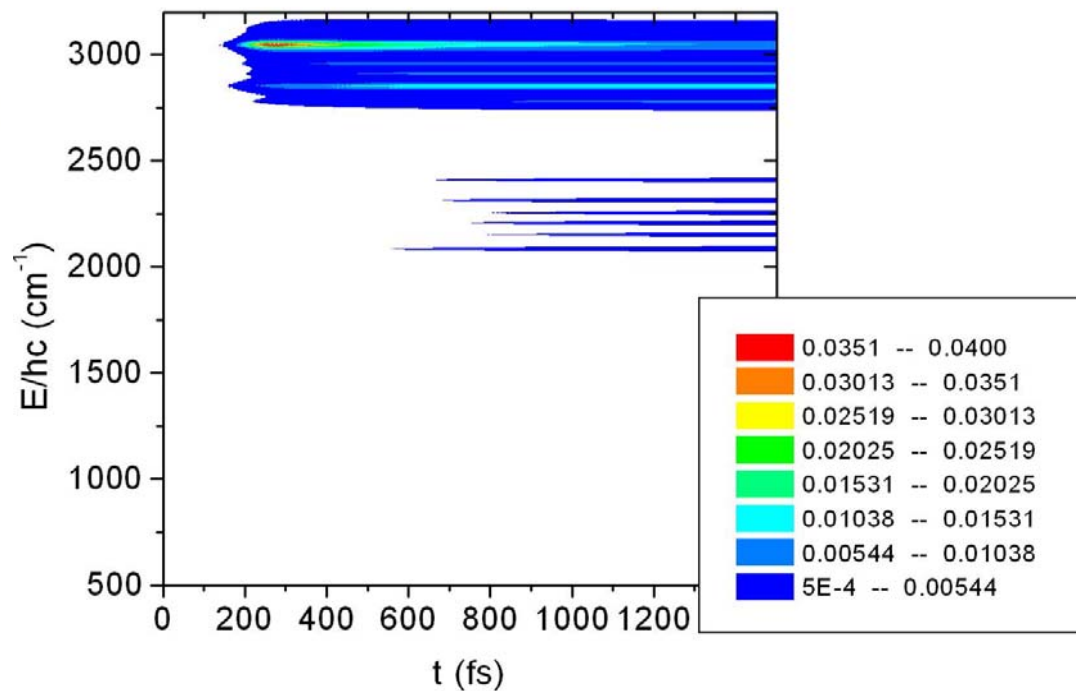


# RELAXATION MODELS



relaxation via bending modes

relaxation via HB-mode



# SUMMARY

quantum chemistry

Quantum Master Equation

classical MD

vibrational relaxation pathways in H-bonds

nonlinear IR spectroscopy

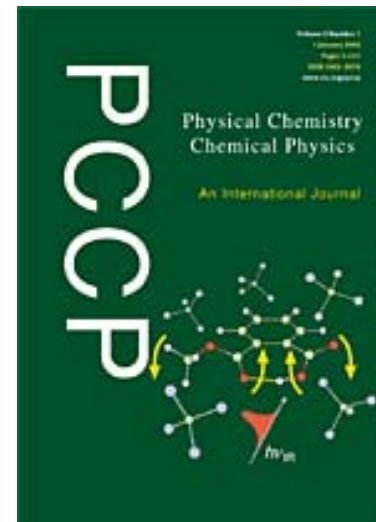
OH-relaxation via in- and out-of-plane bendings

$T_1$  relaxation times

$\nu_{OH} \sim 200\text{fs}$

$\delta_{OH} \sim 800\text{-}900\text{fs}$

$\nu_{HB} \sim 1.6\text{ps}$

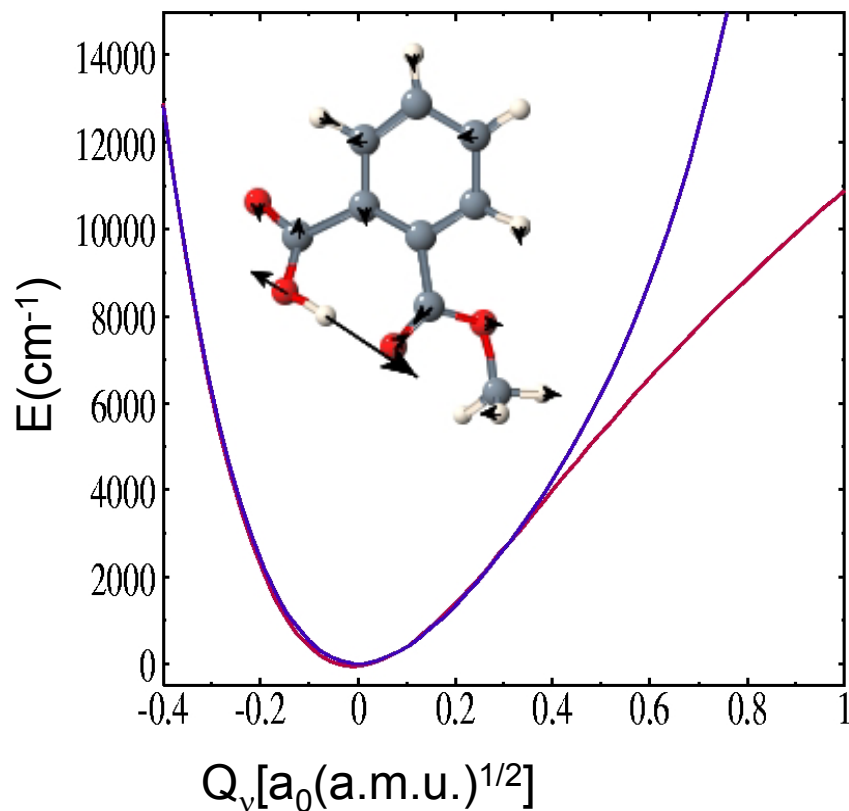




# COHERENT WAVE PACKET MOTION

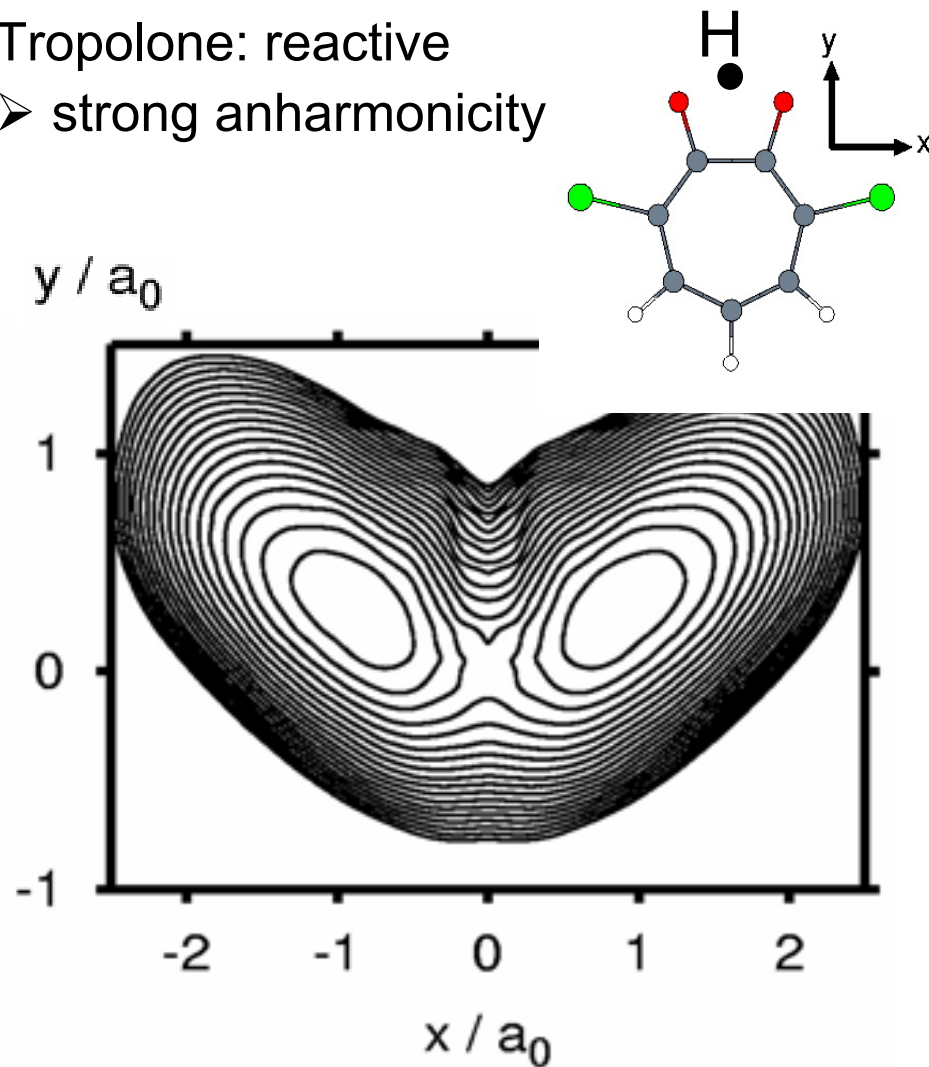
PMME: nonreactive

➤ moderate anharmonicity



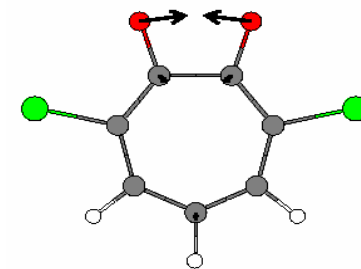
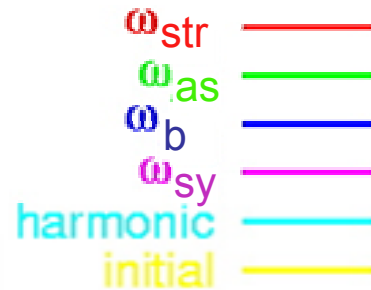
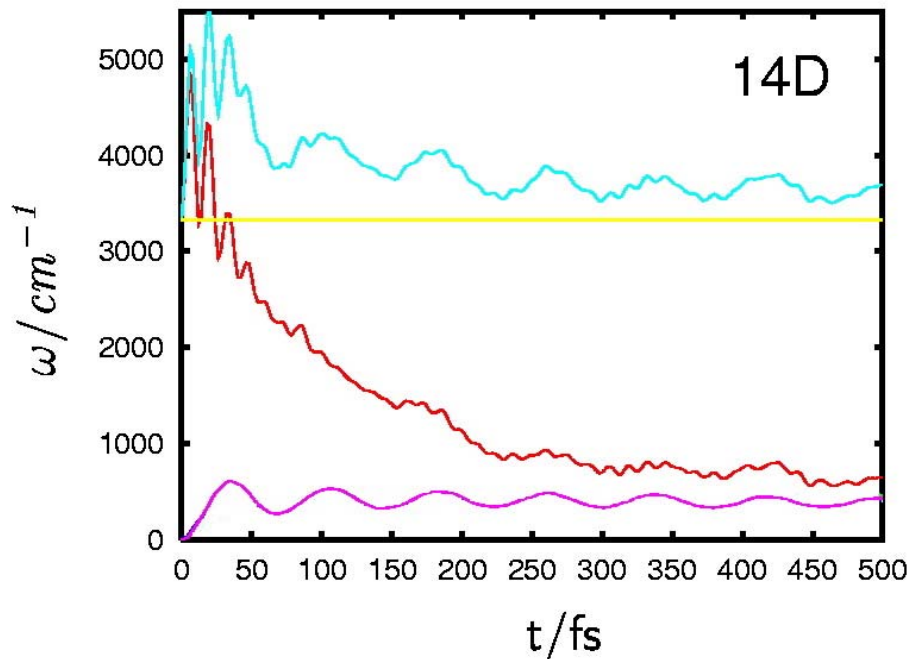
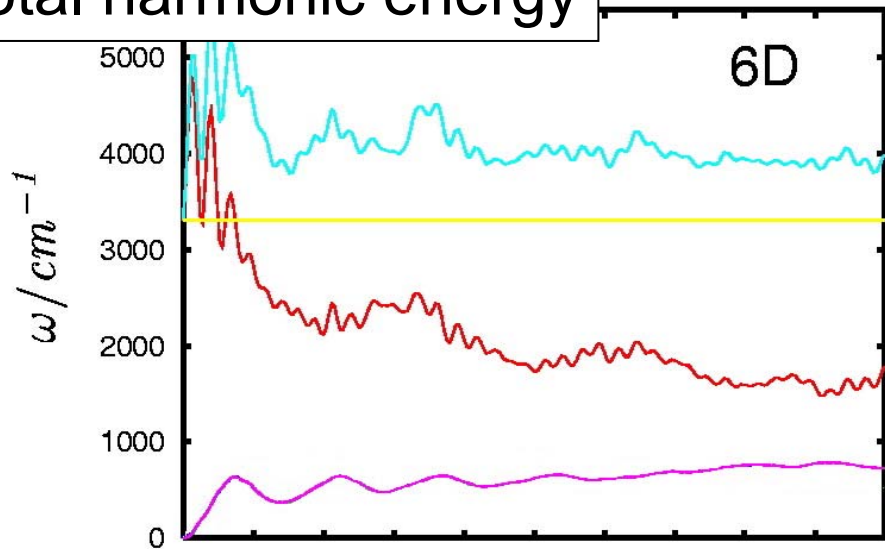
Tropolone: reactive

➤ strong anharmonicity



# H-TRANSFER AND ENERGY FLOW

total harmonic energy



quasi-coherent  
wave packet  
dynamics

# THANKS TO



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